

**Script** generated by TTT

Title: Petter: Compilerbau (21.06.2018)

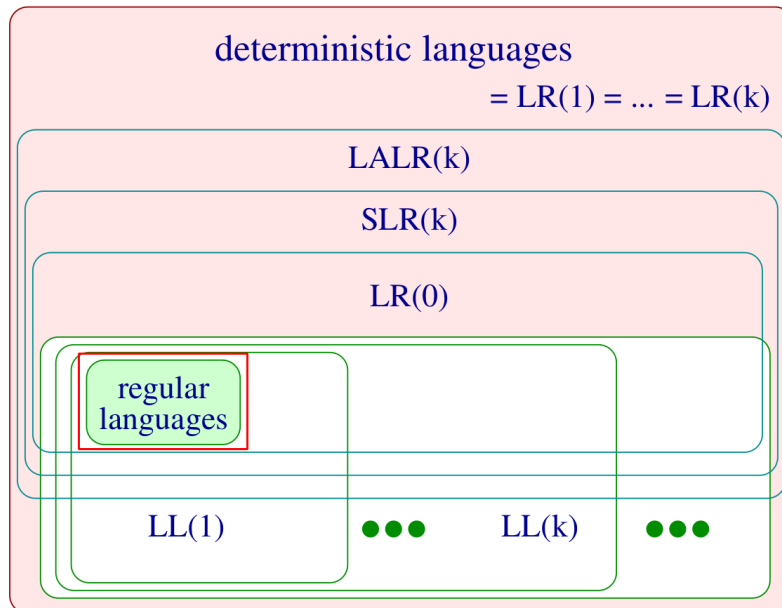
Date: Thu Jun 21 14:15:17 CEST 2018

Duration: 94:19 min

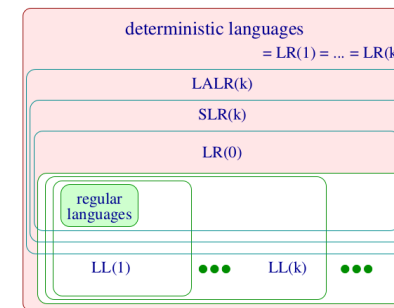
Pages: 47

Chapter 5:  
Summary

Parsing Methods



Parsing Methods

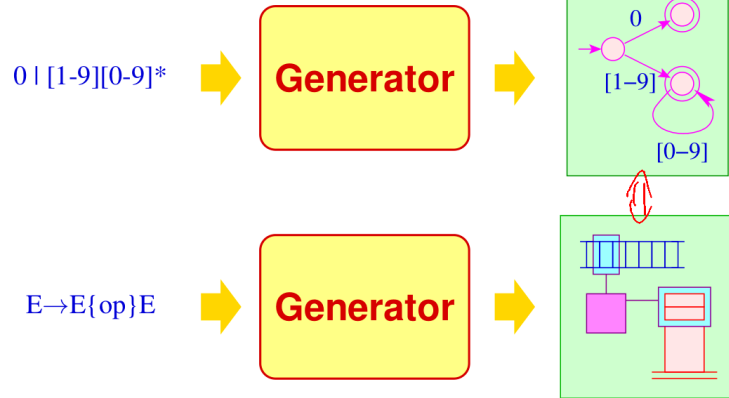


Discussion:

- All contextfree languages, that can be parsed with a deterministic pushdown automaton, can be characterized with an **LR(1)**-grammar.
- **LR(0)**-grammars describe all **prefixfree** deterministic contextfree languages
- The language-classes of **LL(k)**-grammars form a **hierarchy** within the deterministic contextfree languages.

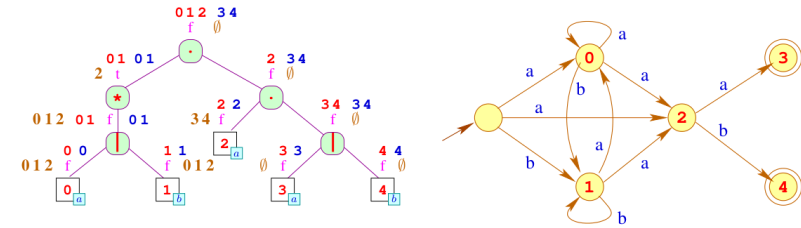
# Lexical and Syntactical Analysis:

Concept of specification and implementation:

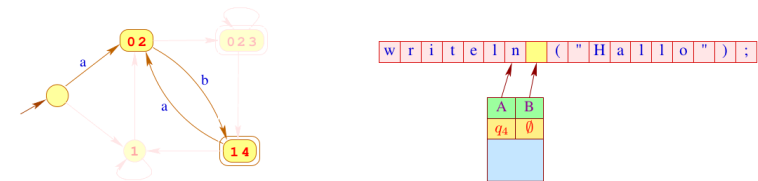


# Lexical and Syntactical Analysis:

From Regular Expressions to Finite Automata



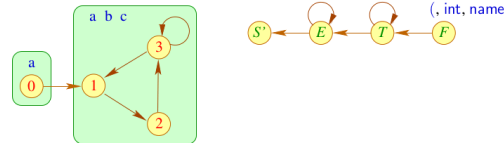
From Finite Automata to Scanners



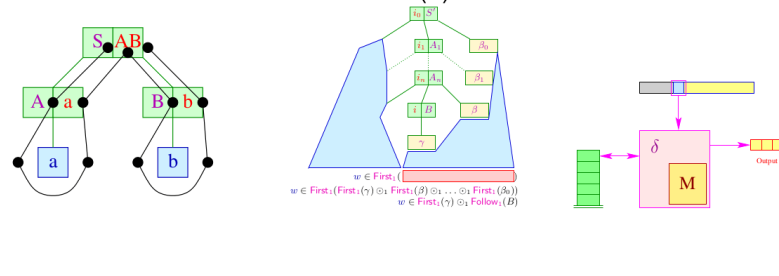
# Lexical and Syntactical Analysis:

Computation of lookahead sets:

$$\begin{aligned}
 F_+(S') &\supseteq F_+(E) & F_+(E) &\supseteq F_+(E) \\
 F_+(E) &\supseteq F_+(T) & F_+(T) &\supseteq F_+(T) \\
 F_+(T) &\supseteq F_+(F) & F_+(F) &\supseteq \{ (, \text{name}, \text{int} \}
 \end{aligned}$$

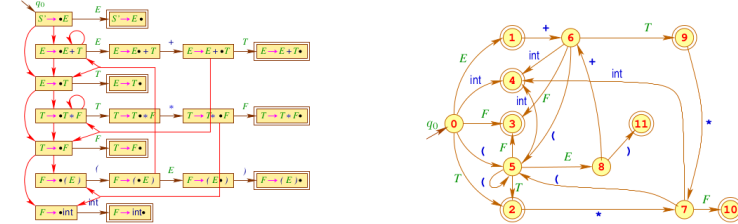


From Item-Pushdown Automata to LL(1)-Parsers:

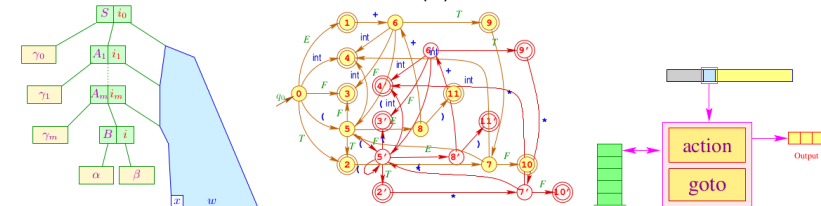


# Lexical and Syntactical Analysis:

From characteristic to canonical Automata:



From Shift-Reduce-Parsers to LR(1)-Parsers:



## Topic: Semantic Analysis

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### Attribute Grammars

- many computations of the semantic analysis as well as the code generation operate on the syntax tree
- what is computed at a given node only depends on the *type* of that node (which is usually a non-terminal)
- we call this a *local* computation:
  - only accesses already computed information from neighbouring nodes
  - computes new information for the current node and other neighbouring nodes

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## Chapter 1: Attribute Grammars

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### Attribute Grammars

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#### Definition attribute grammar

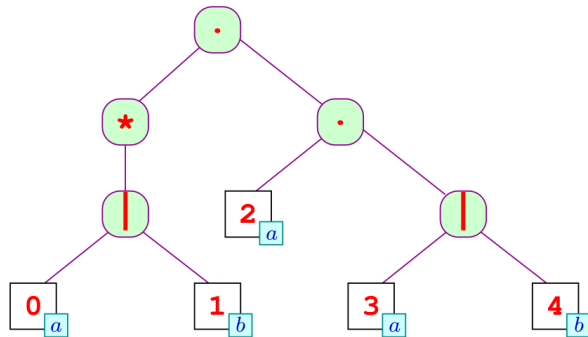
An *attribute grammar* is a CFG extended by

- a set of attributes for each non-terminal and terminal
- local attribute equations

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## Example: Computation of the $\text{empty}[r]$ Attribute

Consider the syntax tree of the regular expression  $(a|b)^*a(a|b)$ :



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## Implementation Strategy

- attach an attribute  $\text{empty}$  to every node of the syntax tree
- compute the attributes in a *depth-first post-order* traversal:
  - at a leaf, we can compute the value of  $\text{empty}$  without considering other nodes
  - the attribute of an inner node only depends on the attribute of its children
- the  $\text{empty}$  attribute is a *synthetic* attribute
- The *local* dependencies between the attributes are dependent on the *type* of the node

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in general:

### Definition

An attribute is called

- *synthetic* if its value is always propagated upwards in the tree (in the direction leaf  $\rightarrow$  root)
- *inherited* if its value is always propagated downwards in the tree (in the direction root  $\rightarrow$  leaf)

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## Attribute Equations for $\text{empty}$

In order to compute an attribute *locally*, we need to specify attribute equations for each node.

These equations depend on the *type* of the node:

for leaves:  $r \equiv \boxed{i \mid x}$  we define  $\text{empty}[r] = (x \equiv \epsilon)$ .

otherwise:

$$\begin{aligned}
 \text{empty}[r_1 \mid r_2] &= \text{empty}[r_1] \vee \text{empty}[r_2] \\
 \text{empty}[r_1 \cdot r_2] &= \text{empty}[r_1] \wedge \text{empty}[r_2] \\
 \text{empty}[r_1^*] &= t \\
 \text{empty}[r_1?] &= t
 \end{aligned}$$

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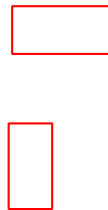
# Specification of General Attribute Systems

## General Attribute Systems

In general, for establishing attribute systems we need a flexible way to refer to parents and children:

~> We use consecutive indices to refer to neighbouring attributes

- $attribute_k[0]$  : the attribute of the current root node
- $attribute_k[i]$  : the attribute of the  $i$ -th child ( $i > 0$ )



# Observations

- the *local* attribute equations need to be evaluated using a *global* algorithm that knows about the dependencies of the equations
- in order to construct this algorithm, we need
  - a sequence in which the nodes of the tree are visited
  - a sequence within each node in which the equations are evaluated
- this *evaluation strategy* has to be compatible with the *dependencies* between attributes



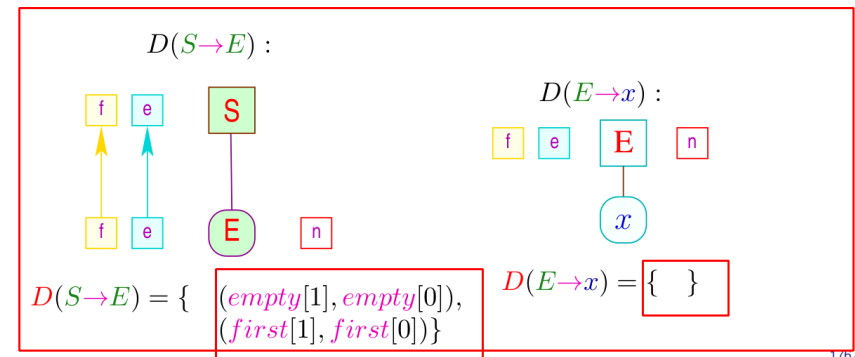
# Observations

- in order to infer an evaluation strategy, it is not enough to consider the *local* attribute dependencies at each node
- the evaluation strategy must also depend on the *global* dependencies, that is, on the information flow between nodes
- the global dependencies thus change with each new syntax tree
- in the example, the parent node is always depending on children only
  - ~> a depth-first post-order traversal is possible
- in general, variable dependencies can be much *more complex*

# Simultaneous Computation of Multiple Attributes

Computing *empty*, *first*, *next* from regular expressions:

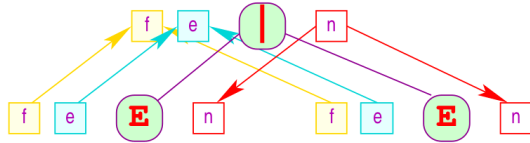
$$\begin{aligned}
 S \rightarrow E : & \quad \begin{aligned} & \text{empty}[0] := \text{empty}[1] \\ & \text{first}[0] := \text{first}[1] \\ & \text{next}[1] := \emptyset \end{aligned} \\
 E \rightarrow x : & \quad \begin{aligned} & \text{empty}[0] := (x \equiv \epsilon) \\ & \text{first}[0] := \{x \mid x \neq \epsilon\} \end{aligned} \\
 & \quad \quad \quad // \text{ (no equation for next) }
 \end{aligned}$$



## Regular Expressions: Rules for Alternative

$$E \rightarrow E|E : \begin{array}{l} \text{empty}[0] := \text{empty}[1] \vee \text{empty}[2] \\ \text{first}[0] := \text{first}[1] \cup \text{first}[2] \\ \text{next}[1] := \text{next}[0] \\ \text{next}[2] := \text{next}[0] \end{array}$$

$D(E \rightarrow E|E) :$



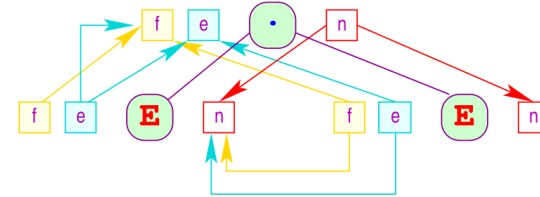
$$D(E \rightarrow E|E) = \{ \begin{array}{l} (\text{empty}[1], \text{empty}[0]), \\ (\text{empty}[2], \text{empty}[0]), \\ (\text{first}[1], \text{first}[0]), \\ (\text{first}[2], \text{first}[0]), \\ (\text{next}[0], \text{next}[2]), \\ (\text{next}[0], \text{next}[1]) \end{array} \}$$

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## Regular Expressions: Rules for Concatenation

$$E \rightarrow E \cdot E : \begin{array}{l} \text{empty}[0] := \text{empty}[1] \wedge \text{empty}[2] \\ \text{first}[0] := \text{first}[1] \cup (\text{empty}[1] ? \text{first}[2] : \emptyset) \\ \text{next}[1] := \text{first}[2] \cup (\text{empty}[2] ? \text{next}[0] : \emptyset) \\ \text{next}[2] := \text{next}[0] \end{array}$$

$D(E \rightarrow E \cdot E) :$



$$D(E \rightarrow E \cdot E) = \{ \begin{array}{l} (\text{empty}[1], \text{empty}[0]), \\ (\text{empty}[2], \text{empty}[0]), \\ (\text{empty}[2], \text{next}[1]), \\ (\text{empty}[1], \text{first}[0]), \\ (\text{first}[1], \text{first}[0]), \\ (\text{first}[2], \text{first}[0]), \\ (\text{first}[2], \text{next}[1]), \\ (\text{next}[0], \text{next}[2]), \\ (\text{next}[0], \text{next}[1]) \end{array} \}$$

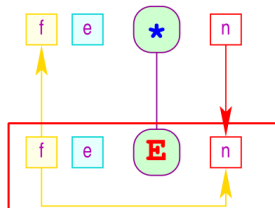
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## Regular Expressions: Kleene-Star and '?'

$$E \rightarrow E^* : \begin{array}{l} \text{empty}[0] := t \\ \text{first}[0] := \text{first}[1] \\ \text{next}[1] := \text{first}[1] \cup \text{next}[0] \end{array}$$

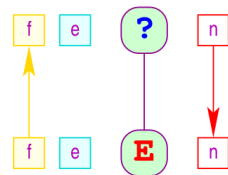
$$E \rightarrow E? : \begin{array}{l} \text{empty}[0] := t \\ \text{first}[0] := \text{first}[1] \\ \text{next}[1] := \text{next}[0] \end{array}$$

$D(E \rightarrow E^*) :$



$$D(E \rightarrow E^*) = \{ \begin{array}{l} (\text{first}[1], \text{first}[0]), \\ (\text{first}[1], \text{next}[2]), \\ (\text{next}[0], \text{next}[1]) \end{array} \}$$

$D(E \rightarrow E?) :$



$$D(E \rightarrow E?) = \{ \begin{array}{l} (\text{first}[1], \text{first}[0]), \\ (\text{next}[0], \text{next}[1]) \end{array} \}$$

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## Challenges for General Attribute Systems

### Static evaluation

Is there a static evaluation strategy, which is generally applicable?

- an evaluation strategy can only exist, if for *any* derivation tree the dependencies between attributes are **acyclic**
- it is **DEXPTIME-complete** to check for cyclic dependencies [Jazayeri, Odgen, Rounds, 1975]

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## Challenges for General Attribute Systems

### Static evaluation

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### Ideas

- 1 Let the *User* specify the strategy
- 2 Determine the strategy dynamically
- 3 Automate *subclasses* only

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## Subclass: Strongly Acyclic Attribute Dependencies

The 2-ary operator  $L[i]$  *re-decorates* relations from  $L$

$$L[i] = \{(a[i], b[i]) \mid (a, b) \in L\}$$

$\pi_0$  projects only onto relations between *root elements only*

$$\pi_0(S) = \{(a, b) \mid (a[0], b[0]) \in S\}$$



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## Subclass: Strongly Acyclic Attribute Dependencies

*Idea:* For all nonterminals  $X$  compute a set  $\mathcal{R}(X)$  of relations between its attributes, as an *overapproximation of the global dependencies* between root attributes of every production for  $X$ .

Describe  $\mathcal{R}(X)$ s as sets of relations, similar to  $D(p)$  by

- setting up each production  $X \mapsto X_1 \dots X_k$ 's effect on the relations of  $\mathcal{R}(X)$
- compute effect on all so far accumulated evaluations of each rhs  $X_i$ 's  $\mathcal{R}(X_i)$
- iterate until stable

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## Subclass: Strongly Acyclic Attribute Dependencies

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$$\pi_0(S) = \{(a, b) \mid (a[0], b[0]) \in S\}$$

*root-projects* the *transitive closure* of relations from the  $L_i$ s and  $D(p)$

$$[[p]]^\#(L_1, \dots, L_k) = \pi_0((D(p) \cup L_1[1] \cup \dots \cup L_k[k])^+)$$

$\mathcal{R}$  maps symbols to relations (global attributes dependencies)

$$\mathcal{R}(X) = \bigcup \{ [[p]]^\#(\mathcal{R}(X_1), \dots, \mathcal{R}(X_k)) \mid p : X \rightarrow X_1 \dots X_k \} \mid X \in N$$

$$\mathcal{R}(X) \supseteq \emptyset \quad \mid X \in N \quad \wedge \quad \mathcal{R}(a) = \emptyset \quad \mid a \in T$$

### Strongly Acyclic Grammars

The system of inequalities  $\mathcal{R}(X)$

- characterizes the class of strongly acyclic Dependencies
- has a unique least solution  $\mathcal{R}^*(X)$  (as  $[[\cdot]]^\#$  is monotonic)

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## Subclass: Strongly Acyclic Attribute Dependencies

### Strongly Acyclic Grammars

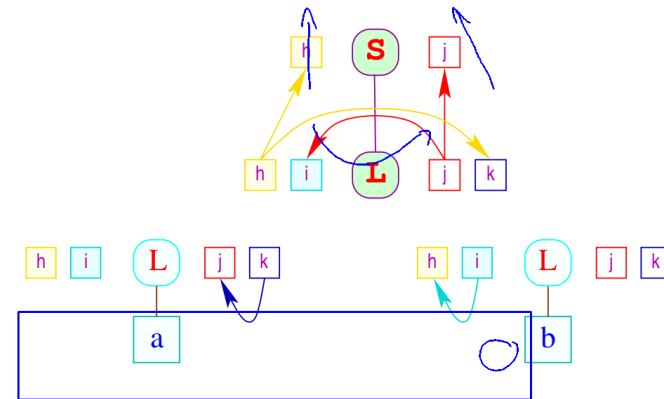
If all  $D(p) \cup \mathcal{R}^*(X_1)[1] \cup \dots \cup \mathcal{R}^*(X_k)[k]$  are acyclic for all  $p \in G$ ,  $G$  is strongly acyclic.

**Idea:** we compute the least solution  $\mathcal{R}^*(X)$  of  $R(X)$  by a fixpoint computation, starting from  $\mathcal{R}(X) = \emptyset$ .

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## Example: Strong Acyclic Test

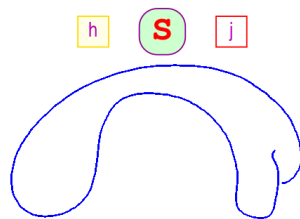
Given grammar  $S \rightarrow L, L \rightarrow a \mid b$ . Dependency graphs  $D_p$ :



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## Example: Strong Acyclic Test

Continue with  $\mathcal{R}(S) = \llbracket S \rightarrow L \rrbracket^+ (\mathcal{R}(L))$ :

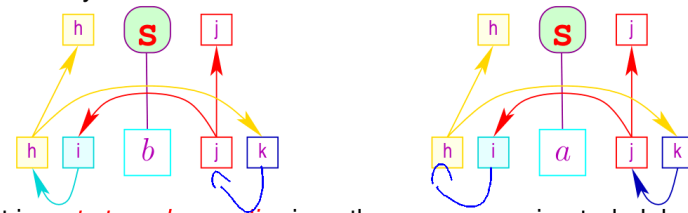


- 1 re-decorate and embed  $\mathcal{R}(L)[1]$
- 2 transitive closure of all relations  $(D(S \rightarrow L) \cup \{(k[1], j[1])\} \cup \{(i[1], h[1])\})^+$
- 3 apply  $\pi_0$
- 4  $\mathcal{R}(S) = \{\}$

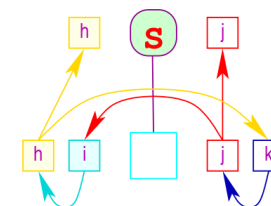
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## Strong Acyclic and Acyclic

The grammar  $S \rightarrow L, L \rightarrow a \mid b$  has only two derivation trees which are both acyclic:



It is *not strongly acyclic* since the over-approximated global dependence graph for the non-terminal  $L$  contributes to a cycle when computing  $\mathcal{R}(S)$ :



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# From Dependencies to Evaluation Strategies

Possible strategies:

# Linear Order from Dependency Partial Order

Possible *automatic* strategies:

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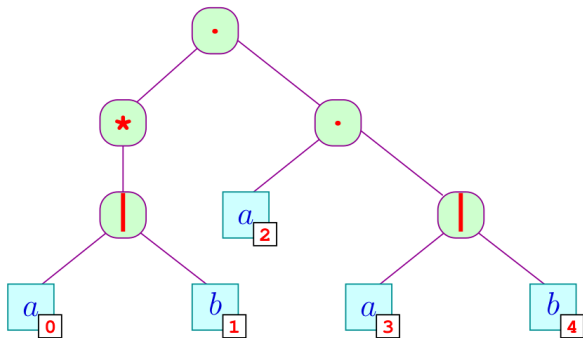
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## Example: Demand-Driven Evaluation

Compute *next* at leaves  $a_2, a_3$  and  $b_4$  in the expression  $(a|b)*a(a|b)$ :

$|$  :  $next[1] := next[0]$   
 $next[2] := next[0]$

$\cdot$  :  $next[1] := first[2] \cup (empty[2] ? next[0] : \emptyset)$   
 $next[2] := next[0]$



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## Demand-Driven Evaluation

### Observations

- each node must contain a pointer to its parent
  - *only required* attributes are evaluated
  - the evaluation sequence depends – in general – on the actual syntax tree
  - the algorithm must track which attributes it has already evaluated
  - the algorithm may visit nodes more often than necessary
- ~ the algorithm is *not local*



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## Evaluation in Passes

**Idea:** traverse the syntax tree several times; each time, evaluate all those equations  $a[i_a] = f(b[i_b], \dots, z[i_z])$  whose arguments  $b[i_b], \dots, z[i_z]$  are evaluated as-of-yet

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## Evaluation in Passes

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### Strongly Acyclic Attribute Systems'

attributes have to be evaluated for each production  $p$  according to

$$D(p) \cup \mathcal{R}^*(X_1)[1] \cup \dots \cup \mathcal{R}^*(X_k)[k]$$

### Implementation

- determine a sequence of child visitations such that the most number of attributes are possible to evaluate
  - in each pass at least one new attribute is evaluated
    - requires at most  $n$  passes for evaluating  $n$  attributes
    - find a strategy to evaluate more attributes
- ~> optimization problem

**Note:** evaluating attribute set  $\{a[0], \dots, z[0]\}$  for rule  $N \rightarrow \dots N \dots$  may evaluate a different attribute set of its children

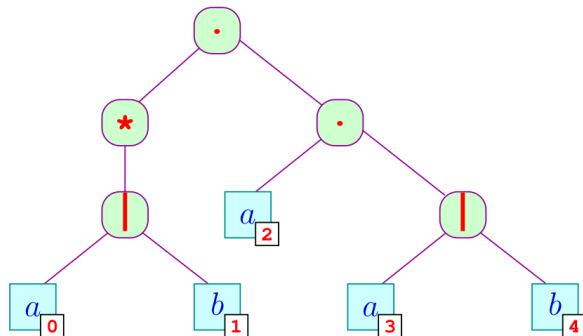
~>  $2^k - 1$  evaluation functions for  $N$  (with  $k$  as the number of attributes)

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## Implementing State

**Problem:** In many cases some sort of state is required.

**Example:** numbering the leaves of a syntax tree



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## Example: Implementing Numbering of Leafs

**Idea:**

- use helper attributes **pre** and **post**
- in **pre** we pass the value for the first leaf down (inherited attribute)
- in **post** we pass the value of the last leaf up (synthetic attribute)

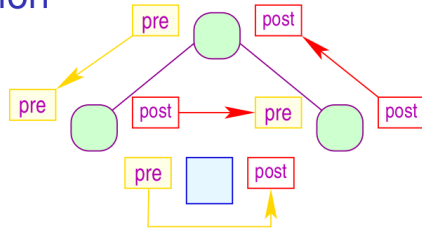
root:  $\text{pre}[0] := 0$   
 $\text{pre}[1] := \text{pre}[0]$   
 $\text{post}[0] := \text{post}[1]$

node:  $\text{pre}[1] := \text{pre}[0]$   
 $\text{pre}[2] := \text{post}[1]$   
 $\text{post}[0] := \text{post}[2]$

leaf:  $\text{post}[0] := \text{pre}[0] + 1$

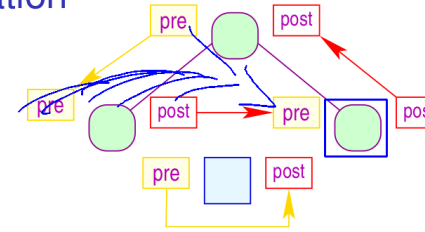
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## L-Attribution



- the attribute system is apparently strongly acyclic

## L-Attribution



- the attribute system is apparently strongly acyclic
- each node computes
  - the inherited attributes before descending into a child node (corresponding to a pre-order traversal)
  - the synthetic attributes after returning from a child node (corresponding to post-order traversal)

### Definition L-Attributed Grammars

An attribute system is *L*-attributed, if for all productions  $S \rightarrow S_1 \dots S_n$  every inherited attribute of  $S_j$  where  $1 \leq j \leq n$  only depends on

- the attributes of  $S_1, S_2, \dots, S_{j-1}$  and
- the inherited attributes of  $S$ .

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## L-Attribution

### Background:

- the attributes of an *L*-attributed grammar can be evaluated during parsing
- important if no syntax tree is required or if error messages should be emitted while parsing
- example: pocket calculator

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## Practical Applications

- symbol tables, type checking/inference, and simple code generation can all be specified using *L*-attributed grammars

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## Implementation of Attribute Systems via a Visitor

- class with a method for every non-terminal in the grammar

```
public abstract class Regex {
    public abstract void accept(Visitor v);
}
```
- attribute-evaluation works via *pre-order / post-order callbacks*

```
public interface Visitor {
    default void pre(OrEx re) {}
    default void pre(AndEx re) {}
    ...
    default void post(OrEx re) {}
    default void post(AndEx re) {}
}
```
- we pre-define a depth-first traversal of the syntax tree

```
public class OrEx extends Regex {
    Regex l, r;
    public void accept(Visitor v) {
        v.pre(this); l.accept(v); v.inter(this);
        r.accept(v); v.post(this);
    }
}
```

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## Example: Leaf Numbering

```
public abstract class AbstractVisitor
    implements Visitor {
    public void pre(OrEx re) { pr(re); }
    public void pre(AndEx re) { pr(re); }
    ...
    public void post(OrEx re) { po(re); }
    public void post(AndEx re) { po(re); }
    abstract void po(BinEx re);
    abstract void in(BinEx re);
    abstract void pr(BinEx re);
}

public class LeafNum extends AbstractVisitor {
    public LeafNum(Regex r) { n.put(r, 0); r.accept(this); }
    public Map<Regex, Integer> n = new HashMap<>();
    public void pr(Const r) { n.put(r, n.get(r)+1); }
    public void pr(BinEx r) { n.put(r.l, n.get(r)); }
    public void in(BinEx r) { n.put(r.r, n.get(r.l)); }
    public void po(BinEx r) { n.put(r, n.get(r.r)); }
}
```

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    public void po(BinEx r) { n.put(r, n.get(r.r)); }
}
```

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folien: bash - Konsole

```
petter@michaels-t420s:~/home/petter$ cd lehre/compilerbau/folien/
petter@michaels-t420s:~/home/petter/lehre/compilerbau/folien$ evince
cb.pdf &
[1] 2224
petter@michaels-t420s:~/home/petter/lehre/compilerbau/folien$
```

Example: Leaf Numbering

```
public abstract class AbstractVisitor
    implements Visitor {
    public void pre(OrEx re) { pr(re); }
    public void pre(AndEx re) { pr(re); }
    ...
    public void post(OrEx re) { po(re); }
    public void post(AndEx re) { po(re); }
    abstract void po(BinEx re);
    abstract void in(BinEx re);
    abstract void pr(BinEx re);
}

public class LeafNum extends AbstractVisitor {
    public LeafNum(Regex r) { n.put(r, 0); r.accept(this); }
    public Map<Regex, Integer> n = new HashMap<>();
    public void pr(Const r) { n.put(r, n.get(r)+1); }
    public void pr(BinEx r) { n.put(r.l, n.get(r)); }
    public void in(BinEx r) { n.put(r.r, n.get(r.l)); }
    public void po(BinEx r) { n.put(r, n.get(r.r)); }
}
```

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Semantic Analysis

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